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Edition

# Prestressed Concrete

A FUNDAMENTAL APPROACH

Fifth Edition  
UPDATE

ACI, AASHTO, IBC 2009 Codes Version

PEARSON

Edward G. Nawy

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